

Simulating Modelica models with a Stand-Alone Quantized State Systems Solver

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Abstract

This article describes an extension of the OpenModelica Compiler that translates regular Modelica models into a simpler language, called Micro-Modelica (μ -Modelica), that can be understood by the recently developed stand-alone Quantized State Systems (QSS) solvers. These solvers are very efficient when simulating systems with frequent discontinuities. Thus, strongly discontinuous Modelica models can be simulated noticeably faster than with the standard discrete time solvers.

The simulation of two discontinuous models is analyzed in order to demonstrate the correctness of the proposed implementation as well as the advantages of using the QSS stand-alone solvers.

Keywords: *OpenModelica, Quantized State Systems, Micro-Modelica, efficient simulation, discontinuous systems*

1 Introduction

There are numerous reasons to desire efficient simulation of hybrid dynamical systems. Nowadays the attention is focused on various aspects of parallelizing the simulation process, while keeping untouched the heart of any simulation pipeline, namely the numerical solver. Indeed, for most researchers and practitioners, the problem of defining an efficient, general-purpose DAE solver is considered to be solved, with DASSL being the default method for all commercial simulation tools. Besides DASSL, there exists a vast variety of solvers targeting different simulation requirements and families of models.

We argue that the attention should be drawn again

to the "basics" and question the underlying assumption of **time discretization** that traditional solvers use. Already at the end of the nineties, Zeigler introduced a new class of algorithms for numerical integration based on **state quantization** and the Discrete Event Simulation (DEVS) formalism [18]. Improving the original approach of Zeigler, Kofman developed a first-order non-stiff **Quantized State System** (QSS) algorithm in 2001 [16], followed later by second- and third-order accurate non-stiff solvers, called QSS2 [13] and QSS3 [15], respectively. Currently, the family of QSS methods includes also stiff system solvers (LIQSS [17]) as well as solvers for marginally stable systems (CQSS [5]).

There is now plenty of evidence that the QSS solvers offer several advantages over the classical approaches [17, 7, 15, 14]. QSS methods allow for **asynchronous** variable updates, a feature particularly suited to real-world sparse systems where a significant reduction of the computational costs is achieved. Furthermore, QSS algorithms inherently provide **dense output**, i.e., they do not need to iterate to detect the discontinuities. They rather predict them. This feature, besides improving on the overall computational performance of these solvers, enables **real-time simulation**. Finally, QSS solvers come with theoretical global error bounds that other solvers lack [4] and recently parallel version of QSS methods have been developed [3].

Originally, QSS algorithms were implemented under DEVS simulation engines such as PowerDEVS [2]. While these implementations were correct, some features of the DEVS engines introduced a large overhead. Recently, a family of stand-alone QSS solvers were developed in order to overcome this issue [6]. The new solvers achieve a speed-up of one order of

magnitude over DEVS implementations.

The stand-alone QSS solvers simulate models described in a C language interface that contains the ODEs and zero crossing functions as well as additional structural information needed by the QSS algorithms. The C interface can be automatically generated from a simple ODE description by a tool developed for that purpose.

Modelica [10, 11] is a multi-domain, modern language for modeling of complex physical systems. It is an object-oriented language built on acausal modeling with mathematical equations and designed to effectively support modular libraries and a standardized model exchange.

There are various commercial environments, such as Dymola, along with open-source implementations, such as OpenModelica [9], that support the Modelica language specification. All of these tools take as input a Modelica model and perform a series of preprocessing steps (model flattening, index reduction, equation sorting and optimization). An optimized DAE representation of the original system is achieved and efficient C++ code is generated to perform the simulation.

There have been previous attempts to simulate Modelica models with QSS algorithms. In [8, 7] an interface between OpenModelica and PowerDEVS (**OMPD interface**) has been implemented and analyzed taking a first step towards using QSS solvers in the simulation of general Modelica models. The interface allows the automatic transformation of large-scale models to the DEVS formalism in a suitable way, thus enabling simulation in the PowerDEVS environment using QSS methods. However, as this interface uses a DEVS engine it suffers from the previously mentioned overhead issues.

In this work, we extended the OpenModelica Compiler (OMC) in order to automatically translate regular Modelica models into a subset of the Modelica language called μ -Modelica. Then, we developed a tool that automatically generates the C interface structure needed by the stand-alone QSS solver from the μ -Modelica description and simulates it. That way, our work enables Modelica users to exploit the benefits of QSS solvers directly from the OpenModelica environment without any further knowledge, using them just like any other traditional solver.

We also conducted an extensive comparative performance analysis between the QSS solvers and OpenModelica DASSL over two discontinuous models. The results show a noticeable improvement in

terms of simulation time and robustness.

The article is organized as follows: Section 2 provides a brief description of the components needed for the solver. Section 3 uncovers the details behind the implemented stand-alone QSS solver, while in Section 4 specific simulation results of two example models are presented and discussed. Finally Section 5 concludes this study, lists open problems and offers directions for future work.

2 Background

2.1 QSS Simulation

Consider a time invariant ODE system:

$$\dot{\mathbf{x}}(t) = \mathbf{f}(\mathbf{x}(t)) \quad (1)$$

where $\mathbf{x}(t) \in \mathbb{R}^n$ is the state vector. The QSS method, [16], approximates the ODE in Eq. 1 as:

$$\dot{\mathbf{x}}(t) = \mathbf{f}(\mathbf{q}(t)) \quad (2)$$

where $\mathbf{q}(t)$ is a vector containing the quantized state variables, which are quantized versions of the state variables $\mathbf{x}(t)$. Each quantized state variable $q_i(t)$ follows a piecewise constant trajectory via the following quantization function with hysteresis:

$$q_i(t) = \begin{cases} x_i(t) & \text{if } |q_i(t^-) - x_i(t)| = \Delta Q_i, \\ q_i(t^-) & \text{otherwise.} \end{cases} \quad (3)$$

where the quantity ΔQ_i is called **quantum**. In other words, the quantized state $q_i(t)$ only changes when it differs from $x_i(t)$ more than ΔQ_i . In QSS, the quantized states $\mathbf{q}(t)$ are following piecewise constant trajectories, and since the time derivatives, $\dot{\mathbf{x}}(t)$, are functions of the quantized states, they are also piecewise constant, and consequently, the states, $\mathbf{x}(t)$, themselves are composed of piecewise linear trajectories.

Unfortunately, QSS is a first-order accurate method only, and therefore, in order to keep the simulation error small, the number of steps performed has to be large.

To circumvent this problem, higher-order methods have been proposed. In QSS2 [13], the quantized state variables evolve in a piecewise linear way with the state variables following piecewise parabolic trajectories. In the third-order accurate extension, QSS3 [15], the quantized states follow piecewise parabolic trajectories, while the states themselves exhibit piecewise cubic trajectories.

QSS methods have Linearly Implicit counterparts (LIQSS1, LIQSS2 and LIQSS3) [17]. The LIQSS methods are explicit (they do not invert matrices or perform iterations) but, under certain conditions, they can efficiently integrate stiff systems.

2.2 Stand-Alone QSS Solvers

The stand-alone QSS solver [6] is a tool that implements the complete QSS family of algorithms without using a DEVS engine.

The tool is composed by two main modules:

1. The simulation engine that integrates the equation $\dot{\mathbf{x}} = \mathbf{f}(\mathbf{q}, t)$ assuming that the quantized state trajectory $\mathbf{q}(t)$ is given.
2. The solvers that given $\mathbf{x}(t)$, effectively calculate $\mathbf{q}(t)$ using the corresponding QSS algorithm.

An important feature of QSS methods is that state variables are updated at different times. Thus, at each simulation step, only some components of $\mathbf{f}(\mathbf{q}, t)$ are evaluated. In consequence, the simulation engine requires the model to be described so that each component of $\mathbf{f}(\mathbf{q}, t)$ can be evaluated separately. Similarly, each zero crossing condition must be given by a separate function together with the corresponding event handler. In addition, structural information describing the dependencies between variables and equations must be provided.

All the simulation framework, including the simulation engine, the solvers and the models are written in plain C.

Since it is very uncomfortable for an end-user to describe a model providing all this information, the QSS solver tool includes a translator that generates the C interface with all the structural information from a regular ODE description.

This ODE description can have the following components:

- ODEs of the form $\dot{x}_j = f_j(\mathbf{x}, \mathbf{a}, \mathbf{d}, t)$ where \mathbf{x} are continuous state, \mathbf{a} are algebraic and \mathbf{d} are discrete state variables
- Algebraic equations of the form $a_j = g_j(\mathbf{x}, \mathbf{a}, \mathbf{d}, t)$ with the restriction that a_j can only depend on a_1, \dots, a_{j-1} .
- Zero crossing functions of the form $z_j = h_j(\mathbf{x}, \mathbf{a}, \mathbf{d}, t)$.

- Associated to each zero crossing function, two handlers (one for positive and the other for negative crossings) where discrete as well as continuous state variables can be updated.

This description is processed by a parser that computes all the structure, including

- the incidence matrices from continuous and discrete state variables to ODE equations,
- the incidence matrices from continuous and discrete state variables to zero crossing functions,
- the incidence matrices from handlers to ODE equations and zero crossing functions.

This information is then used by a code generator that produces the C interface describing the model.

3 Simulation of Modelica Models with Stand-Alone QSS Methods

As we mentioned above, the stand-alone QSS solver has a tool to extract the structural information from a simple ODE description. In order to exploit this feature, we first developed a language called μ -Modelica and then we extended the stand-alone QSS parser so it understands this language and converts it into the ODE description used by the stand-alone QSS solver.

Then, we extended the OMC so that it generates μ -Modelica models from regular Modelica models.

In this way, regular Modelica models can be automatically simulated by the stand-alone QSS solvers.

In Figure 1 we see the complete compilation and simulation process involved.

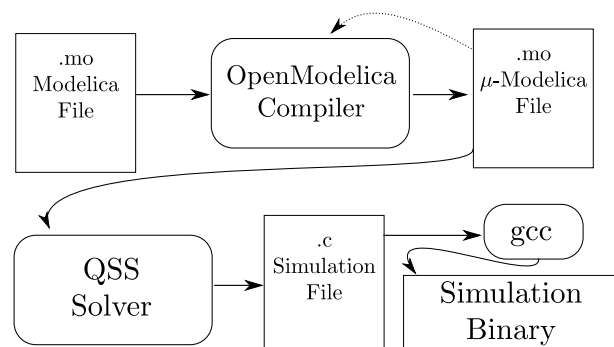


Figure 1: Pipeline of the compilation/simulation process

Below, we first introduce the μ -Modelica language and then we describe the translation process from Modelica to μ -Modelica

3.1 The μ -Modelica subset

The language μ -Modelica was defined to be a subset of Modelica as close as possible to the ODE description accepted by the stand-alone QSS solver. μ -Modelica contains only the necessary Modelica keywords and structures to define an ODE based hybrid model.

The μ -Modelica language has the following restrictions:

- The model is in a flat form, i.e. no classes are allowed.
- All variables are `Real` and there are only three classes of variables: continuous states (`x[]`), discrete states (`d[]`) and algebraics (`a[]`).
- Parameters also belong to class `Real` and they can have arbitrary names.
- Equations are given in explicit ODE form.
- An algebraic variable `a[i]` can only depend on previously defined algebraic variables (`a[1:i-1]`).
- Discontinuities are expressed only by `when` clauses inside the `algorithm` section. Conditions on `when` clauses can only be relations (`<`, `≤`, `>`, `≥`) and, inside the clauses, only assignment of discrete state variables (`d[]`) and `reinit`s are allowed.

This restricted language is not meant to be used by an end user, but only as an intermediate language between OpenModelica and the QSS solver. The end user is supposed to use the complete Modelica language and then use the OMC to get a μ -Modelica file.

3.2 Simulating μ -Modelica models with the stand-alone QSS solver

As we mentioned above, the QSS solver includes a parser that extracts all the structural information from an ODE representation.

This parser was extended in order to understand μ -Modelica language. After this extension, the parser performs the following actions:

- It recognizes Modelica keywords for parameters, and discrete states.

- It takes equations of the form `der(x[i])=expr()`, generating the corresponding ODE and structural information.
- It recognizes clauses of the form `when expr1>expr2 then`, generating a zero crossing function `zc=expr1-expr2` with a handler for the positive crossing containing the expressions that are found inside the clause. If it then finds a clause `elsewhen expr1<expr2 then`, it generates the handler for the negative crossing.
- It also generates the structural information corresponding to the zero-crossing functions and the handlers.

3.3 Converting Modelica models to μ -Modelica

In order to complete the process to simulate regular Modelica models with the stand alone QSS solver, we added a new output target for the OMC to generate μ -Modelica models.

Most of the work is done by what OMC already does without any modification: It first simplifies expressions, sorts the equations and transforms the DAE into an ODE, producing the necessary code for solving the algebraic loops. It also recognizes zero crossing conditions.

Thus, we take the structures generated by OMC and process them as follows:

1. Find the continuous state variables (those where the `der` operator is used), algebraic variables (those solved in the ODE equation that are not states), and discrete state variables (those defined as discrete, including `Integer` and `Boolean` variables.). Boolean variables are replaced by real valued variables where `1.0` is true and `0.0` is false.
2. Parameter names are changed replacing dot(s) for underscore(s). This is done for all identifiers.
3. Continuous state, discrete state and algebraic variables (`Real x[]`, `Real d[]`, `Real a[]`) are defined and code is generated with their initial values.
4. In each equation of the ODE section, each appearance of continuous state, discrete state and algebraic variables is replaced by their corresponding μ -Modelica alias `x[]`, `a[]` or `d[]`.

5. If the equation is part of an algebraic loop, an external solving C function is generated and a call to that function is generated in the μ -Modelica.
6. For each zero crossing function, when and elsewhen clauses are generated. The extra elsewhen is necessary to assign different values to the discrete state variable associated with the crossing function.
7. when clauses are emitted also replacing continuous states, algebraic and discrete state variables in the condition and in the body of the clause.
8. sample operators are expanded using an extra discrete state variable.
9. elsewhen clauses are emitted as regular when in the algorithm section.

For example a model of a bouncing ball in Modelica:

```
model bball1
  Real y(start = 1),v,a;
  Boolean flying(start = true);
  parameter Real m = 1;
  parameter Real g = 9.8;
  parameter Real k = 10000;
  parameter Real b = 10;
equation
  der(y) = v;
  der(v) = a;
  flying = y>0;
  a = if flying then -g else -g -
    - (b * v + k * y)/m;
end bball1;
```

would be translated to μ -Modelica as follows:

```
model bball1
  constant Integer N = 2;
  Real x[N](start=xinit());
  discrete Real d[1](start=dinit());
  Real a[1];
  parameter Real m = 1.0;
  parameter Real g = 9.8;
  parameter Real k = 10000.0;
  parameter Real b = 10.0;
  function xinit
    output Real x[N];
  algorithm
    x[2]:= 1.0 /* y */;
    x[1]:= 0.0 /* v */;
  end xinit;
  function dinit
    output Real d[1];
  algorithm
```

```
    d[1]:= (1.0) /* flying */;
  end dinit;
/* Equations */
equation
  der(x[2]) = x[1];
  a[1] = -d[1] * g + (1.0 - d[1]) *
    (((-b) * x[1] + (-k) * x[2]) / m - g);
  der(x[1]) = a[1];
algorithm
/* Discontinuities */
  when x[2] > 0.0 then
    d[1] := 1.0;
  elsewhen x[2] < 0.0 then
    d[1] := 0.0;
  end when;
end bball1;
```

We see easily that the model has two continuous states, one algebraic and one discrete state variable together with a discontinuity on $x[2]$ that updates the discrete state.

When the original Modelica model contains an algebraic loop, it will be detected by OMC and μ -Modelica will include a piece of code of the form

```
...
function fsolve15
  input Real i0;
  input Real i1;
  output Real o0;
  output Real o1;
  output Real o2;
  external "C" ;
end fsolve15;
...
equation
...
(a[1],a[2],a[3])=fsolve15(x[2],d[1])
```

together with a C function that solves the loop using GNU Scientific Library (GSL) [12].

This call indicates that variables $a[1:3]$ are computed by a simple C external function, so the QSS parser treats it as a regular function for obtaining the structural information.

In the mentioned external function we improved what was done by OMC taking into account a feature of linear algebraic loops. A linear algebraic equation usually has the form $A \cdot z = b$ (with z being the unknown), where A usually depends on discrete state variables only. Thus, when the change in the continuous state variable only affects the term b , then it is not necessary to invert matrix A in that step.

4 Examples and Simulation Results

In this section we analyze the results obtained using the tools presented in this work.

4.1 Benchmark Framework

As benchmark problems we focused on two systems exhibiting heavily discontinuous behavior, namely a buck converter and a DC-DC buck interleaved circuit. All models were constructed using the Modelica Standard Library 3.1 and can be downloaded from [1].

For each of the examples we used the modified OMC (r11645) to generate the corresponding μ -Modelica model and then the QSS solver to simulate them. In each case, we compare the run-time efficiency and accuracy of the QSS methods against the standard DASSL solver of OpenModelica v1.8.1.

In order to measure the execution time for each simulation algorithm, the reported simulation time from each environment was used. Although OpenModelica provides several ways to measure the CPU time needed for simulation (including a profiler) we observed significant differences in the reported timings. After consulting the OpenModelica developers we finally used `time ./model_executable -lv LOG_STATS` to measure the pure simulation time. We note here that the timing results obtained this way are significantly smaller than the "official" simulation time reported in the OMSHELL or the profiler. Therefore, the speedups we get can be considered to be rather conservative.

Testing has been carried out on a Dell 32bit desktop with a quad core processor @ 2.66 GHz and 4 GB of RAM and in a Intel i7-970 (32 bits) @ 3.20GHz and 2 GB of RAM.

The measured CPU time should not be considered as an absolute ground-truth since it will vary from one computer system to another, but the relative ordering of the algorithms is expected to remain the same.

Calculating the accuracy of the simulations can only be performed approximately, since the state trajectories of the models cannot be computed analytically. To estimate the accuracy of the simulation algorithms for a given setting, reference trajectories ($\mathbf{t}^{\text{ref}}, \mathbf{y}^{\text{ref}}$) have to be obtained. To this end, the LIQSS2 solver was used with a tight tolerance of 10^{-7} .

To calculate the simulation error, each simulated

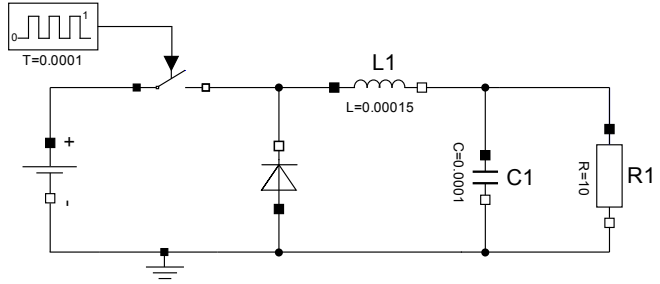


Figure 2: Buck Circuit

trajectory was compared against the reference solution. To achieve this goal, we forced all solvers to output points on the same equidistant grid obtaining simulation trajectories ($\mathbf{t}^{\text{ref}}, \mathbf{y}^{\text{sim}}$) without changing the integration step. Then, the normalized mean absolute error is calculated as:

$$\text{error} = \frac{\text{mean}(|\mathbf{y}^{\text{sim}} - \mathbf{y}^{\text{ref}}|)}{\text{mean}(|\mathbf{y}^{\text{ref}}|)} \quad (4)$$

4.2 Buck circuit

In Figure 2, a DC-DC converter circuit, known as *Buck Circuit*, is sketched. The circuit has two continuous state variables, namely the current through the inductor L1 and the voltage across the capacitor C1. The presence of the switch introduces hybrid behavior to the system. For the simulation error we focus on the C1.V state variable. The model was simulated for 0.01 sec. and the ground-truth trajectory can be seen in Fig 3.

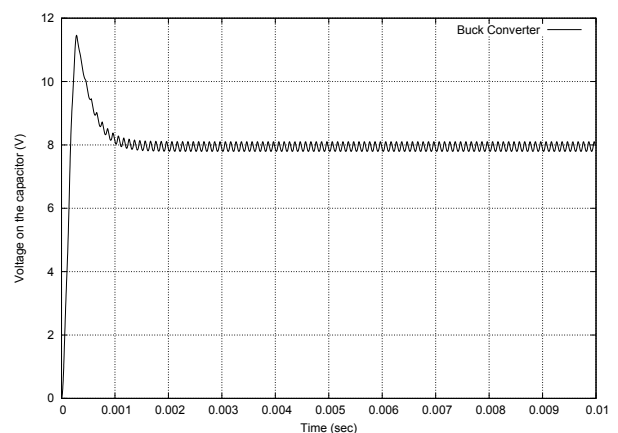


Figure 3: Buck Circuit - Simulation

Initially we simulated the model in OMC using the default number of 500 output points. We observed

that the DASSL solver in OMC fails to detect and handle correctly the events. On the other hand, when we forced OMC to output more points the error decreases because the extra evaluation needed to generate the output forces DASSL to re-evaluate the zero crossing functions, thus detecting the events. This is why we compared OMC's native DASSL solver with different precisions and different number of output points against the QSS solver using the stiff LIQSS2 and LIQSS3 methods. The results are summarized in Table 1.

Indeed we observe that for 500 output points the DASSL solver in OMC doesn't manage to reduce the achieved error when tightening the precision requirements, a clear sign that it fails to simulate correctly the model. When the output points are increased to 10000 the OMC results get closer to the ground-truth trajectory and the error is reduced.

Therefore, it makes sense to compare the runtime efficiencies for the case of 10000 points where we clearly see that QSS methods are more efficient than DASSL in OMC. To perform the simulation for an achieved error of the order of 10^{-5} , LIQSS3 required 12 msec while DASSL needed 74 msec. Therefore, **the use of the LIQSS3 solver instead of the standard DASSL in OpenModelica speeds up the simulation by a factor of 6x.** The achieved reduction in both simulation accuracy and time is depicted graphically in Fig. 4. The results are plotted in a log-log plot where the closer the lines are to the origin the better the corresponding algorithm performs.

Performing an internal comparison between the QSS methods, we see that the third-order LIQSS3 method is slightly more efficient than LIQSS2, especially when the tolerance requirement, thus the achieved error, gets smaller. This is expected, since the LIQSS2 solver needs to take smaller steps compared to LIQSS3 to reach the desired accuracy (e.g. for an error of 10^{-6} LIQSS2 needs 53391 steps while LIQSS3 only used 11314). **Thus, we can conclude that the third-order LIQSS3 algorithm should be preferred for practical applications.** We see also that as QSS algorithms provide dense output, the number of output points does not affect the simulation timings.

Finally, another characteristic of the QSS methods is evident from the obtained results. We verify that in general DASSL performs significantly less steps than any of the QSS methods. However, each one of these steps is much more complicated and time-consuming than the ones performed in a QSS solver, as it in-

volves -in general- estimation of the whole function $f(\cdot)$. On the other hand, each step in QSS updates one state variable, therefore requiring the evaluation of the corresponding $f_i(\cdot)$. As the simulated systems get bigger, more complex and sparse, evaluating $f_i(\cdot)$ is much more efficient than the global $f(\cdot)$.

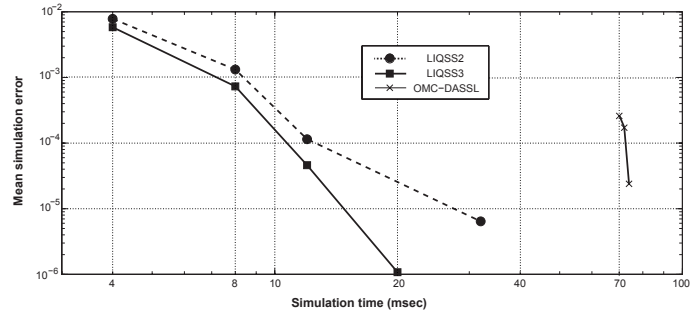


Figure 4: CPU time vs Error for the buck converter model (10000 output points)

4.3 Interleaved DC-DC Circuit

Figure 5 depicts the model of an interleaved buck converter. This circuit is similar to the buck converter analyzed above but it contains several switching sections that are activated at different times in order to reduce the output voltage ripple. In this case, we consider a circuit with four branches.

To build this model, all the components were taken from the MSL 3.1, except for the booleanDelay that implements a boolean delay that outputs its received boolean input after a fixed period T. The delay has no memory, i.e. when an input is received, any scheduled output is cancelled and overwritten by the new input.

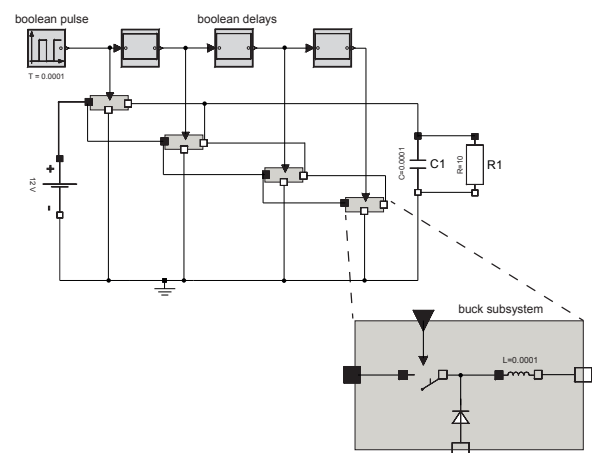


Figure 5: DC-DC interleaved circuit

We have simulated this model for 0.01 sec. again

Table 1: This table depicts the simulation results of various solvers for the buck converter circuit for a requested simulation time of 0.01 sec. The comparison performed includes required CPU time (in msec), number of steps taken, as well as the simulation accuracy relative to the reference trajectory obtained with LIQSS2 and tolerance of 10^{-7} .

			500 output points			10000 output points		
			CPU time (msec)	Steps	Simulation Error	CPU time (msec)	Steps	Simulation Error
QSS	LIQSS3	10^{-2}	4	3351	5.84E-03	4	3351	5.83E-03
	LIQSS3	10^{-3}	8	4163	7.31E-04	8	4163	7.32E-04
	LIQSS3	10^{-4}	12	6804	4.60E-05	12	6804	4.61E-05
	LIQSS3	10^{-5}	20	11314	1.07E-06	20	11314	1.08E-06
	LIQSS2	10^{-2}	4	3863	7.83E-03	4	3863	7.84E-03
	LIQSS2	10^{-3}	8	6715	1.32E-03	8	6715	1.32E-03
	LIQSS2	10^{-4}	12	18519	1.15E-04	12	18519	1.15E-04
	LIQSS2	10^{-5}	32	53391	6.42E-06	32	53391	6.42E-06
OpenModelica	DASSL	10^{-3}	22	4273	3.56E-03	70	5249	2.66E-04
	DASSL	10^{-4}	28	5636	3.17E-03	72	5955	1.75E-04
	DASSL	10^{-5}	32	7781	3.28E-03	74	7623	2.40E-05

focusing on the capacitor voltage, getting the simulated trajectory seen in Fig 6. The same experiments as for the buck circuit case were performed and listed in Table 2 where we made the same comparisons as in the previous example (Sec 4.2).

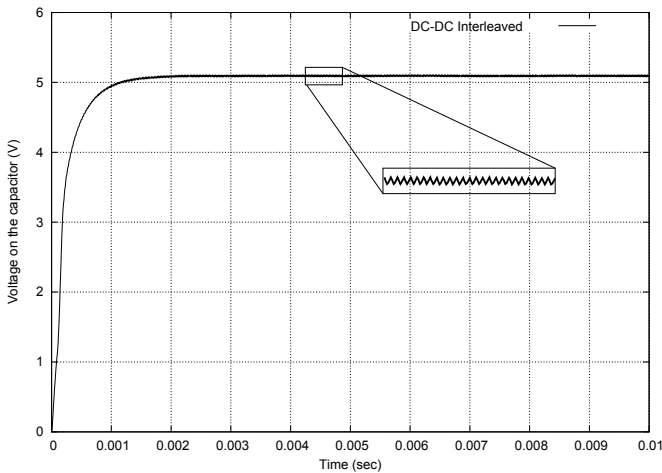


Figure 6: DC-DC Interleaved - Simulation

We see from Fig. 7 that for obtaining a mean error of the order of 10^{-3} OpenModelica’s DASSL takes 488 msec while it takes LIQSS2 12 msec and 60 msec for LIQSS3. **This shows 40x and 8x speedups for LIQSS2 and LIQSS3.** The difference in timings between LIQSS2 and LIQSS3 is because the implementation of LIQSS3 is not yet completely optimized and some problems are still present. Also, when asking

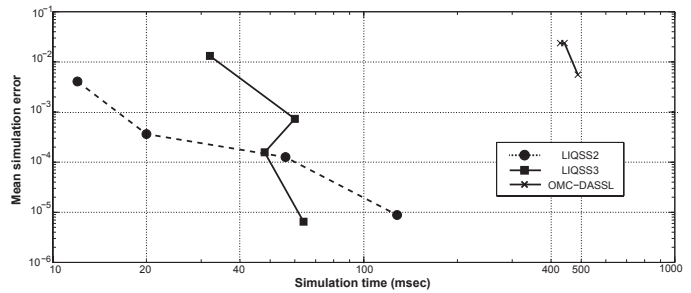


Figure 7: CPU time vs Error for the DC-DC interleaved model (10000 output points)

the QSS solver for 10000 number of output points, neither the error nor the number of steps changes because of the dense output.

In Figure 8 we show the different steady state values obtained with different setups. We see that the discontinuity detection of OMC is heavily influenced by the number of output steps. Here we included Dymola 6.0 result in order to provide a generally-accepted ground-truth solution. We note here that no timing measurements were conducted with Dymola.

5 Conclusion and Future Work

In this article, the integration of the novel stand-alone QSS solvers in the OpenModelica environment is presented and analyzed. The implementation has been tested successfully for both correctness and efficiency in simulating real-world Modelica models.

Table 2: This table depicts the simulation results of various solvers for the DC-DC interleaved circuit for a requested simulation time of 0.01 sec. The comparison performed includes required CPU time (in msec), number of steps taken, as well as the simulation accuracy relative to the reference trajectory obtained with LIQSS2 and tolerance of 10^{-7} .

		500 output points			10000 output points		
		CPU time (msec)	Steps	Simulation Error	CPU time (msec)	Steps	Simulation Error
QSS	LIQSS3 10^{-2}	32	18396	1.32E-02	32	18396	1.32E-02
	LIQSS3 10^{-3}	60	33426	7.31E-04	60	33426	7.31E-04
	LIQSS3 10^{-4}	48	29408	1.57E-04	48	29408	1.57E-04
	LIQSS3 10^{-5}	64	39951	6.48E-06	64	39951	6.48E-06
	LIQSS2 10^{-2}	12	10715	4.08E-03	12	10715	4.08E-03
	LIQSS2 10^{-3}	20	29082	3.63E-04	20	29082	3.63E-04
	LIQSS2 10^{-4}	56	73218	1.26E-04	56	73218	1.26E-04
	LIQSS2 10^{-5}	128	198001	8.80E-06	128	198001	8.80E-06
OpenModelica	DASSL 10^{-3}	310	14421	4.96E-02	428	17571	2.37E-02
	DASSL 10^{-4}	363	22375	5.03E-02	442	18574	2.37E-02
	DASSL 10^{-5}	496	31387	5.41E-02	488	23625	5.57E-03

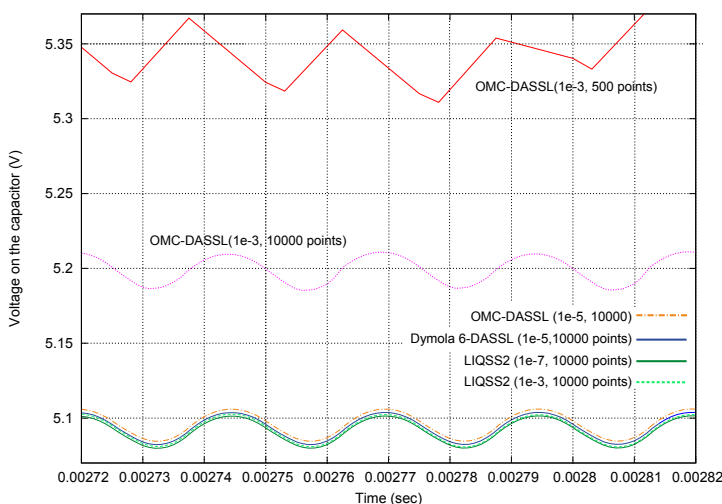


Figure 8: Comparison of the final steady state for different setups

Comparisons on two example models were performed, demonstrating the increased efficiency of the stiff LIQSS solvers over the default DASSL solver of OpenModelica. **Consistent speedups were achieved and the required CPU time was reduced up to 40 times.** Furthermore, for the two systems simulated we observed that the default DASSL solver failed to generate the correct results if we didn't force many output points. Increasing the number of output points, though, means increasing the number of steps taken by the DASSL algorithm, thus the computation time. On the other hand, not only the QSS solvers

simulated correctly the models at all setups but, because of the dense output they inherently generate, the number of steps taken remains constant regardless of how many output points are requested.

However, there still remain open problems to be addressed in the future. First of all, our proposed solution was tested on few examples. A larger set of models has to be simulated and tested for correctness, as well as efficiency, of the implementation. In particular, we should focus on large-scale hybrid models because their dynamics should uncover the power and efficiency of QSS methods. To this end, the μ -Modelica has to be extended to handle more complex systems.

An interesting line of research could be the utilization of the μ -Modelica language as an intermediate language to enable other tools to include Modelica models. Its simplicity makes the burden on the compiler a lot lighter.

The ultimate goal is to integrate the family of QSS solvers (by use of the μ -Modelica translation step) in OpenModelica as native solvers. To achieve this the QSS solver should generate output results in the format expected by the OpenModelica environment. Finally, we need to note that work is also ongoing on improving the QSS solver itself.

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